x:	7	8	9	10
y:	3	1	1	9

5. Attempt any two parts of the following:

 $(2\times10=20)$ 

(a) Factorize the matrix:

$$A = \begin{bmatrix} 5 & -2 & 1 \\ 7 & 1 & -5 \\ 3 & 7 & 4 \end{bmatrix}$$

in the form LU, where L is the lower triangular matrix and U is the unit upper triangular matrix and hence solve the system of equations:

$$5x-2y+z=4$$
;  $7x+y-5z=8$ ;  $3x+7y+4z=10$ .

(b) (i) Find f'(5) from the following table:

х:	0	1	2	3	4	5
f(x):	4930	5026	5122	5217	5312	5407

(ii) The acceleration of a rocket which is launched from the ground is given according to time t as follows:

t(sec.)	0	10	20	30	40
f(m/sec <sup>2</sup> )	30	31.63	33.34	35.47	37.75

t(sec.)	50	60	70	80
$f(m/sec^2)$	40.33	43.25	46.69	50.67

Find the velocity of the rocket at t = 80 sec using Simpson's 1/3 rule.

(c) Find the value of y(1.1) using Runge-Kutta method of fourth order for the differential equation:

$$\frac{dy}{dx} = y^2 + xy$$
,  $y(1) = 1.0$ 

Take h = 0.05.

**EAS401** 

(Following Paper ID and Roll No. to be filled in your Answer Book)
PAPER ID: 3987 Roll No.

## B. Tech.

## (SEM. IV) THEORY EXAMINATION 2011-12 MATHEMATICS—III

Tir · · 3 Hours

Total Marks : 100

- Note: (1) Attempt all questions. Marks are indicated against each question.
  - (2) Provide the statistical tables which are required by the students.
- Attempt any four parts of the following:  $(4\times5=20)$ 
  - (a) Define analytic function. Discuss the analyticity and differentiability of  $f(z) = |z|^4$  at z = 0.
  - (b) Define conjugate harmonic function. Find the analytic function f(z) = u + iv whose real part is  $u(x, y) = (x y)(x^2 + 4xy + y^2)$ .
  - (c) Evaluate  $\oint_C \frac{1}{z^2 \sin z} dz$ , where C is the triangle with

vertices (0, 1), (2, -2) and (7, 1).

- (d) Verify Cauchy's theorem for  $f(z) = z^2 + 3z + 2$  where C is the perimeter of square with vertices  $1 \pm i$ ,  $-1 \pm i$ .
- (e) Expand  $f(z) = \frac{z}{(z^2-1)(z^2+4)}$  in Laurent series in 1 < |z| < 2.
- (f) Use contour integration to evaluate:

$$\int_{-\infty}^{\infty} \frac{x^2 dx}{(x^2 + 1)^2}$$

- 2. Attempt any four parts of the following: (4×5=20)
  - (a) Define moment generating function. Find the moment generating function of a random variable X whose probability function is given by:

$$P(X = x) = p(1-p)^x, x = 0, 1, 2, ...., \infty.$$

- (b) In two frequency distributions the second moments about mean are 36 and 49 respectively while third moments about mean are 43.2 and 85.75. Compare the skewness in the two frequency distributions.
- (c) Fit the curve  $y = ae^{bx}$  to the following data:

x:	1	2	3	4	5	6
y:	15.3	20.5	27.4	36.6	49.1	65.6

(d) Calculate Karl Pearson's coefficient of correlation for the following data:

x:	11	10	09	08	07	06	05
y:	20	18	12	8	10	5	4

- (e) The line of regression of marks in Statistics (x) on the marks in Accountancy (y) for a class of 50 students is 3y 5x + 180 = 0. Average marks in Accountancy is 44 and variance of marks in Statistics is <sup>9</sup>/<sub>16</sub> of variance of marks in Accountancy. Find (i) the average marks in Statistics and (ii) coefficient of correlation between marks of both subjects.
- (f) A candidate is called for an interview by three companies. For the first company, there are 12 candidates and for the second there are 15 candidates and for the third, there are 10 candidates. What are the chances of his getting at least one of the companies?
- 3. Attempt any two parts of the following: (2×10=20)
  - (a) In a Poisson distribution with unity mean, show that the mean deviation from mean is (2/e) times the standard deviation.

(b) The figures of production (in Lakh tonne) of a sugar factory are given below:

Year	1999	2000	2001	2002	2003	2004	2005
Pr oduction	7.7	8.8	9.4	8.5	9.1	9.8	9.0

Fit a straight line by the method of least square and show the trend values. Also determine the monthly increase in production.

- (c) The areas are of two types, urban and rural and two parties A and B participated in the election. The random sample consists of 33 individuals from rural areas of whom 18 voted in favour of party A and 27 individuals from urban areas of whom 12 voted in favour of party A. Use Chi-square test to examine whether the nature of area is related to voting preference. (Given that the value of Chi-square at 5% for 1 d.f. = 3.84).
- 4. Attempt any *four* parts of the following:  $(4\times5=20)$ 
  - (a) Find the smallest positive root of  $x^4 x = 10$  correct to three decimal places using Regula-Falsi method.
  - (b) Use Newton-Raphson method to find the root of  $3x \log_{10} x = 6$ , correct to four decimal places.
  - (c) Define central difference operator, shift operator and the average operators. Establish  $\mu\delta = \frac{1}{2}(E E^{-1})$ .
  - (d) Fit a polynomial of degree 3 and hence determine y(3.5) for the following data:

x:	3	4	5	6
y:	6	24	60	120

(e) Use Newton's Divided difference formula to compute f(8) for the following data:

x:	3	7	9	10
<b>f(x)</b> :	168	120	72	63